

$$\frac{y^3}{y^3} = y^{3-3} = y^0 \quad \frac{\omega^2}{\omega^6} = \omega^{2-6} = \omega^{-4}$$

$\frac{y^3}{y^3} = 1$

Def: $x^0 = 1, x \neq 0.$

Rem: $\frac{0}{0} = \text{undefined}$

$\frac{a}{b} = c$ is the same thing as $a = bc$

$$\frac{2}{2} = 1$$

$$10 = 2(5)$$

$$\frac{0}{0} = 2$$

$$0 = 0 \cdot 2 = 0$$

$$\frac{0}{0} = 4$$

$$0 = 0 \cdot 4 = 0$$

$$\frac{g^2}{g^7} = g^{2-7} = g^{-5}$$

$$\frac{g \cdot g}{\cancel{g \cdot g} \cdot \cancel{g} \cdot \cancel{g} \cdot \cancel{g} \cdot \cancel{g} \cdot \cancel{g} \cdot \cancel{g}} = \frac{1}{g^5}$$

Def: $x^{-n} = \frac{1}{x^n}$

EX:

$$w^{-2} = \frac{1}{w^2}$$

$$g^{-1} = \frac{1}{g}$$

$$c^{-6} = \frac{1}{c^6}$$

$$\frac{1}{u^{-3}} = u^3, \frac{1}{u^3}$$

$$\begin{aligned}
 u^{-3} &= \frac{1}{u^3} = \frac{\cancel{1}}{\cancel{1} \cdot u^3} \\
 &= \frac{1}{u^3} \cdot \frac{u^3}{1} = \frac{1 \cdot u^3}{u^3 \cdot 1} = \frac{u^3}{u^3} = \frac{u^3}{1} = u^3
 \end{aligned}$$

Power of a Quotient Rule

If n is a positive integer and a and c are real numbers, then

$$\left(\frac{a}{c}\right)^n = \frac{a^n}{c^n}, \quad c \neq 0$$

Quotient Rule for Exponents

If m and n are positive integers and a is a real number, then

$$\frac{a^m}{a^n} = a^{m-n}$$

as long as a is not 0.

Zero Exponent

$a^0 = 1$, as long as a is not 0.

Ex: (p 310)

$$2. -3^2 = (-1) 3^2 = (-1) 9 = -9$$

$$4. (-3)^2 = (-3)(-3) = 9$$

$$6. -4^3 = (-1) 4^3 = -64$$

$$8. (-4)^3 = (-4)(-4)(-4) = -64$$

$$\begin{aligned} 28. \quad y^2 \cdot y^1 &= y^3 \\ 30. \quad (-5)^7 \cdot (-5)^6 &= (-5)^{13} = -5^{13} \\ 32. \quad (-2z^3)(-2z^2) &= 4z^5 \\ 34. \quad (a^2b)(a^{13}b^{17}) &= a^{15}b^{18} \\ 36. \quad (-7a^3b^3)(7a^{19}b) &= -49a^{22}b^4 \\ 38. \quad (12x^5)(-x^6)(x^4) &= -12x^{15} \end{aligned}$$

$$\begin{aligned}
44. (ab)^6 &= a^6 b^6 \\
46. (4x^6)^2 &= 16x^{12} \\
48. (a^4b)^7 &= a^{28} b^7 \\
50. (-3x^7yz^2)^3 &= -27x^{21}y^3z^6 \\
52. \left(\frac{q}{t}\right)^{11} &= \frac{q^{11}}{t^{11}} \\
54. \left(\frac{xy}{7}\right)^2 &= \frac{x^2y^2}{49} \\
56. \left(\frac{xy^4}{-3z^3}\right)^3 &= -\frac{x^3y^{12}}{27z^9}
\end{aligned}$$

$$62. \frac{y^{10}}{y^9} = y^1$$

$$64. \frac{(-6)^{13}}{(-6)^{11}} = (-6)^2 = 36$$

$$66. \frac{x^8 y^6}{x y^5} = x^7 y$$

$$68. \frac{9a^4 b^7}{27ab^2} = \frac{a^3 b^5}{3} \text{ or } \frac{1}{3} a^3 b^5$$

$$70. 23^0 = 1$$

$$72. (4y)^0 = 1$$

$$74. -2x^0 = -2(1) = -2$$

$$76. -3^0 + 4^0 = -1 + 1 = 0$$

78. $(-9)^2$

80. $\left(\frac{2}{3}\right)^3$

82. $\left(\frac{pt}{3}\right)^3$

86. $(3y^4)(-5y)$

88. $(y^2z^2)(y^{15}z^{13})$

90. $(-3s^5t)(-7st^{10})$

5.2: Adding and Subtracting Polynomials

Expression, term

Coefficient

Polynomial

A **polynomial in x** is a finite sum of terms of the form ax^n , where a is a real number and n is a whole number.

Types of Polynomials

A **monomial** is a polynomial with exactly one term.

A **binomial** is a polynomial with exactly two terms.

A **trinomial** is a polynomial with exactly three terms.

Degree of a Term

The degree of a term is the sum of the exponents on the variables contained in the term.

Ex: (p 320)

Find the degree of a polynomial

Find the value of each polynomial when (a) $x = 0$ and (b) $x = -1$. See Examples 4 and 5.

16. $x^2 - 4$

18. $-2x^3 + 3x^2 - 6$

Simplify

24. $18x^3 - 4x^3$

32. $\frac{1}{6}x^4 - \frac{1}{7}x^2 + 5 - \frac{1}{2}x^4 - \frac{3}{7}x^2 + \frac{1}{3}$

Perform the Following:

36. $(3x^2 + 7) + (3x^2 + 9)$

40. $(5x^2 + 4) - (-2y^2 + 4)$

44. $(-7x^2 + 4x + 7) - (-8x + 2)$

46.
$$\begin{array}{r} 7x^3 + 3 \\ +2x^3 + 1 \\ \hline \end{array}$$

48.
$$\begin{array}{r} 5u^5 - 4u^2 + 3u - 7 \\ -(3u^5 + 6u^2 - 8u + 2) \\ \hline \end{array}$$

60. $(6y^5 - 6y^3 + 4) + (-2y^5 - 8y^3 - 7)$

62. $(-a^2 + 1) - (a^2 - 3) + (5a^2 - 6a + 7)$

68. Subtract $(5y + 7x^2)$ from the sum of $(8y - x)$ and $(3 + 8x^2)$.

70. Subtract $(4x^2 - 2x + 2)$ from the sum of $(x^2 + 7x + 1)$ and $(7x + 5)$.

80. $(3x - 2 + 6y) + (7x - 2 - y)$

86. $(3x^2y - 6xy + x^2y^2 - 5) - (11x^2y^2 - 1 + 5yx^2)$

92. $-7x(x)$

94. $6r^3(7r^{10})$

96. $-z^2y(11zy)$

5.3: Multiplying Polynomials

Ex: (p 327)

2. $9t^6(-3t^5)$

4. $(-5.2x^4)(3x^4)$

6. $\left(-\frac{3}{4}y^7\right)\left(\frac{1}{7}y^4\right)$

8. $(x)(5x^4)(-6x^7)$

18. $-x(6y^3 - 5xy^2 + x^2y - 5x^3)$

22. $(x + 2)(x + 9)$

24. $(y - 10)(y + 11)$

26. $\left(x + \frac{3}{5}\right)\left(x - \frac{2}{5}\right)$

28. $(5x^2 + 2)(6x^2 + 2)$

34. $(x^2 + 4)^2$

38. $(x + 3)(x^2 + 5x - 8)$

42. $(3 + b)(2 - 5b - 3b^2)$

44. $(y - 1)^3$

46. $(3x + 4)^3$

50. $(4x - 5)(8x^2 + 2x - 4)$

52. $(3x^2 - x + 2)(x^2 + 2x + 1)$

56. $-5x(x^2 - 3x + 10)$

60. $\left(m + \frac{2}{9}\right)\left(m - \frac{1}{9}\right)$

68. $(5x + 4)(x^2 - x + 4)$

70. $(a^2 + 3a - 2)(2a^2 - 5a - 1)$

5.4: Special Products

Ex: (p 334)

4. $(y - 12)(y + 4)$

6. $(3y - 5)(2y - 7)$

12. $(x + 7)^2$

24. $(4x - 5)(4x + 5)$

26. $\left(10x + \frac{2}{7}\right)\left(10x - \frac{2}{7}\right)$

28. $(2x - y)(2x + y)$

36. $(6a + 7)(6a + 5)$

38. $(x - 10)(x + 10)$

42. $(x^3 - 2)(5x + y)$

44. $(x - 2)(x^2 - 4x + 2)$

48. $(11x - 7y)(11x + 7y)$

54. $(x^5 + 5)(x^2 - 8)$

62. $\left(\frac{2}{3}a - b^2\right)\left(\frac{2}{3}a - b^2\right)$

70. $(3x + 5)(3x - 5)$

74. $\left(\frac{a}{2} + 4y\right)\left(\frac{a}{2} - 4y\right)$

78. $(b + 3)(2b^2 + b - 3)$

82. $\frac{x^3y^6}{xy^2}$

84. $\frac{-6a^8y}{3a^4y}$

86. $\frac{-48ab^6}{32ab^3}$

5.5: Negative Exponents & Scientific Notation

Look at division

Negative Exponents

If a is a real number other than 0 and n is an integer, then

$$a^{-n} = \frac{1}{a^n}$$

Negative Exponents

If a is a real number other than 0 and n is an integer, then

$$a^{-n} = \frac{1}{a^n} \quad \text{and} \quad \frac{1}{a^{-n}} = a^n$$

Ex: (p 343)

2. 6^{-2}

8. $\left(\frac{1}{8}\right)^{-2}$

16. $\frac{r^{-5}}{s^{-2}}$

22. $4^{-2} - 4^{-3}$

24. $\frac{-1}{y^{-6}}$

Summary of Exponent Rules

If m and n are integers and a , b , and c are real numbers, then:

Product rule for exponents: $a^m \cdot a^n = a^{m+n}$

Power rule for exponents: $(a^m)^n = a^{m \cdot n}$

Power of a product: $(ab)^n = a^n b^n$

Power of a quotient: $\left(\frac{a}{c}\right)^n = \frac{a^n}{c^n}$, $c \neq 0$

Quotient rule for exponents: $\frac{a^m}{a^n} = a^{m-n}$, $a \neq 0$

Zero exponent: $a^0 = 1$, $a \neq 0$

Negative exponent: $a^{-n} = \frac{1}{a^n}$, $a \neq 0$

Ex: (p 343)

$$46. \frac{-5x^4y^5}{15x^4y^2}$$

$$48. (-5a^4b^{-7})(-a^{-4}b^3)$$

$$52. \left(\frac{a^5b}{a^7b^{-2}}\right)^{-3}$$

$$56. \frac{5^{-1}z^7}{5^{-2}z^9}$$

$$58. \frac{6^{-5}x^{-1}y^2}{6^{-2}x^{-4}y^4}$$

$$60. \left(\frac{r^{-2}s^{-3}}{r^{-4}s^{-3}}\right)^{-3}$$

$$68. \frac{(a^6b^{-2})^4}{(4a^{-3}b^{-3})^3}$$

5.6: Dividing Polynomials

Dividing a Polynomial By a Monomial

Divide each term of the polynomial by the monomial.

$$\frac{a + b}{c} = \frac{a}{c} + \frac{b}{c}, \quad c \neq 0$$

Ex: (p 350)

2. $\frac{15x^2 - 9x^5}{x}$

4. $\frac{8x^3 - 4x^2 + 6x + 2}{2}$

8. $\frac{6x^5 + 3x^4}{3x^4}$

34. $\frac{m^3n^2 - mn^4}{mn}$